

JUURIMHTÄLÖT JA JUURIEPÄHTÄLÖT / slf

Olkoon $a, b \geq 0$

$$a = b \quad || (\)^2$$
$$a^2 = b^2$$
$$a < b \quad || (\)^2$$
$$a^2 < b^2$$

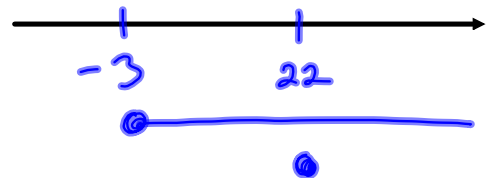
esim $-5 = 5 \quad | (\)^2$ epätosi
 $25 = 25$ tosi

esim a) $\sqrt{x+3} = 5$
myj: $x+3 \geq 0$
 $x \geq -3$

$$\sqrt{x+3} = 5 \quad | (\)^2$$

$$x+3 = 25$$

$$x = 22$$



V: 22

Ex 2

$$\sqrt{x+3} = x \quad | \quad ()^2 \quad \begin{matrix} \text{mj: } x+3 \geq 0 \text{ ju } x \geq 0 \\ \text{ju } x \geq -3 \text{ ju } x \geq 0 \end{matrix}$$

$$x+3 = x^2$$

$$x^2 - x - 3 = 0$$

$$\vdots$$

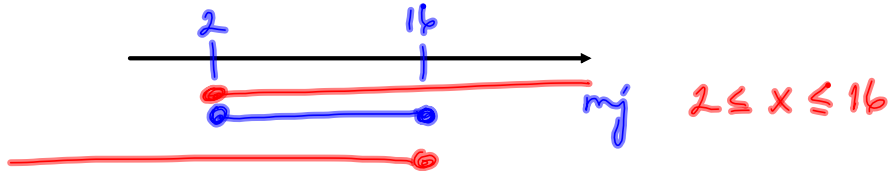
$$x = \frac{1 + \sqrt{13}}{2} \text{ tai } \in \text{mj}$$

$$x = \frac{1 - \sqrt{13}}{2} \notin \text{mj}$$

V: $x = \frac{1 + \sqrt{13}}{2}$

crim3 $\sqrt{x-2} \leq 16-x \quad |(\)^2 \quad 2)$

1) my: $x-2 \geq 0$ ja $16-x \geq 0$
 $x \geq 2$ ja $x \leq 16$



$x-2 \leq (16-x)^2$
 \vdots

$(a-b)^2 = a^2 - 2ab + b^2$

$x^2 - 33x + 258 \geq 0$

merk: f

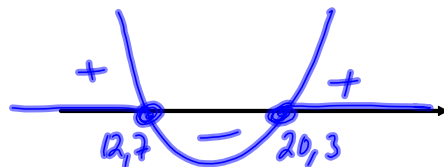
merk. etn: $x^2 - 33x + 259 = 0$

\vdots

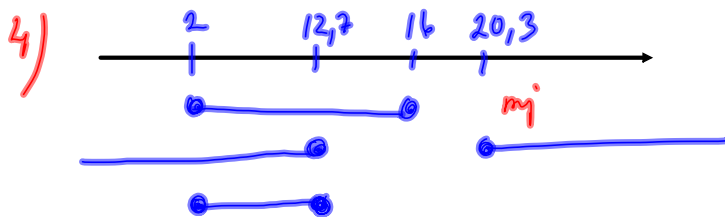
$x = 20,3$

tai

$x = 12,7$



3) $x \leq 12,7$ tai $x \geq 20,3$



$\sqrt{}$: $2 \leq x \leq 12,7$