

$$A = (3, 5) \quad \begin{array}{l} \swarrow \text{LOPPUPISTE} \\ B = (-2, -3) \end{array}$$

a) Muodosta vektori $\vec{AB} = (-2-3)\mathbf{i} + (-3-5)\mathbf{j}$
 $= -5\mathbf{i} - 8\mathbf{j}$

b) Laske sen pituus $|\vec{AB}| = \sqrt{(-5)^2 + (-8)^2}$
 $= \sqrt{25 + 64} = \sqrt{89} \approx$

c) Muodosta yksikkövektori

$$\vec{AB}^\circ = \frac{\vec{AB}}{|\vec{AB}|} = \frac{-5\mathbf{i} - 8\mathbf{j}}{\sqrt{89}} = \frac{-5}{\sqrt{89}}\mathbf{i} - \frac{8}{\sqrt{89}}\mathbf{j}$$

d) Muodosta paikkavektori

$$\vec{OB} = -2\mathbf{i} - 3\mathbf{j}$$

g) AB janan keskeispiste

$$A = (\overset{x}{\underset{\downarrow}{3}}, \overset{y}{\underset{\downarrow}{5}}) \quad B = (\overset{x}{\underset{\downarrow}{-2}}, \overset{y}{\underset{\downarrow}{-3}})$$

$$\text{kp: } \left(\frac{3+(-2)}{2}, \frac{5+(-3)}{2} \right) = \left(\frac{1}{2}, 1 \right)$$

Suoralla
tuoalla

suuntavektori
normaali vektori

$$\frac{\vec{s}}{|\vec{s}|}$$

e) $\vec{CD} = 2\vec{i} - 5\vec{j}$
 Pistetulo $\vec{AB} \cdot \vec{CD}$

$$\begin{aligned}\vec{AB} \cdot \vec{CD} &= \vec{a} \cdot \vec{b} \\ &= -5 \cdot 2 + (-8) \cdot (-5) \\ &= -10 + 40 = 30\end{aligned}$$

f) Näiden välinen kulma

$$\cos \alpha = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| \cdot |\vec{b}|}$$

$$\begin{aligned}|\vec{CD}| = |\vec{b}| &= \sqrt{2^2 + (-5)^2} \\ &= \sqrt{4 + 25} = \sqrt{29}\end{aligned}$$

~~Q~~

$$\cos \alpha = \frac{30}{\sqrt{89} \cdot \sqrt{29}}$$