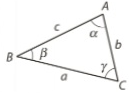
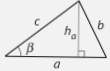

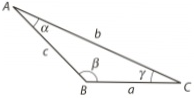
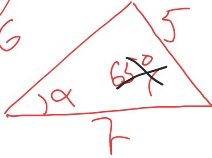


kulmien summa	$\alpha + \beta + \gamma = 180^\circ$	
pinta-ala	$A = \frac{1}{2}ah_a = \frac{1}{2}ac \sin \beta = 2R^2 \sin \alpha \sin \beta \sin \gamma$	
sisään piirretyn ympyrän säde	$r = \frac{2A}{a+b+c}$	
ympäri piirretyn ympyrän säde	$R = \frac{abc}{4A} = \frac{bc}{2h_a} = \frac{a}{2 \sin \alpha} = \frac{b}{2 \sin \beta} = \frac{c}{2 \sin \gamma}$	
Sinilause	$\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma} = 2R$	
Kosinilause (laajennettu Pythagoraan lause)	$a^2 = b^2 + c^2 - 2bc \cos \alpha$	

Esim. Ratkaise kulma α

a)



sinilauseella:

$$\frac{a}{\sin \alpha} = \frac{b}{\sin \beta}$$

$$\frac{6}{\sin \alpha} = \frac{5}{\sin 65^\circ}$$

$$\sin \alpha = \frac{5 \cdot \sin 65^\circ}{6}$$

$$\alpha = \arcsin\left(\frac{5 \cdot \sin 65^\circ}{6}\right) = \underline{\underline{49^\circ}}$$

b) Kosinilauseella:

$$c^2 = a^2 + b^2 - 2ab \cos \alpha$$

$$5^2 = 6^2 + 7^2 - 2 \cdot 6 \cdot 7 \cdot \cos \alpha$$

$$25 - 36 - 49 = -84 \cdot \cos \alpha \quad ||: (-84)$$

$$\cos \alpha = \frac{-60}{-84}$$

$$\alpha = \arccos\left(\frac{60}{84}\right) = \underline{\underline{44,4^\circ}}$$