

Sinin kaavoja!

tähdet ympyrät
 $n \in \mathbb{Z}$

$$\sin x = \sin(x + n2\pi) \quad (\text{tähdet ympyrät mukaan ratkaisuihin})$$

$$\sin(-x) = -\sin x \quad (\text{voit siirtää edessä olevan miinusmerkin sisään})$$

$$\sin x = \sin(\pi - x) \quad (\text{supplem-kuhma mukaan vastaukseen})$$

$$\sin x = \cos\left(\frac{\pi}{2} - x\right)$$

$$\sin\left(\frac{\pi}{2} - x\right) = \cos x$$

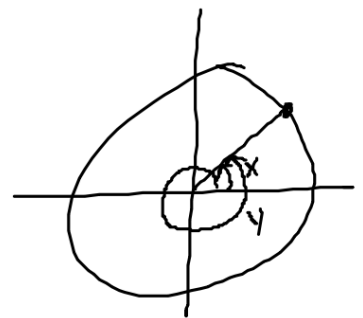
← (voit muuttaa
 $\sin \leftrightarrow \cos$)

$$\sin x = \sin y$$

1. Sama kulma (+ täydelt ymp.)

$$x = y + n2\pi$$

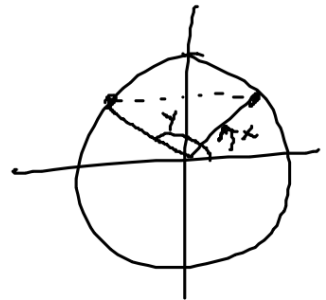
$$x = y + n \cdot 360^\circ$$



2. Kulmat supplementtikulmia

$$x = \pi - y + n2\pi$$

$$x = 180^\circ - y + n360^\circ$$



Esim. $\sin x = \frac{1}{2}$ \leftarrow MAOL:sta $\sin \frac{\pi}{6} = \frac{1}{2}$

$$\sin x = \sin \frac{\pi}{6}$$

$$x = \frac{\pi}{6} + n2\pi$$

tai

$$x = \pi - \frac{\pi}{6} + n2\pi$$

$$x = \frac{5\pi}{6} + n2\pi$$

n kokon-
luku

$$\in \sin \quad \sin x = 0,37$$



$$\sin y = 0,37$$

$$y = \sin^{-1}(0,37) \approx 0,37901$$

$$\sin x = \sin(0,37901)$$

$$x = \underline{0,37901 + n2\pi} \quad \text{for } n \in \mathbb{Z}$$

$$x = \pi - 0,37901 + n2\pi = \underline{2,763 + n2\pi}$$

$$\text{Esin} \cdot 4 \cdot \sin 3x = 1 \quad \parallel :4$$

$$\sin 3x = \frac{1}{4} = \sin(0,25268)$$

\uparrow
 $\gamma = \sin^{-1}(0,25)$

$$3x = 0,25268 + n2\pi \quad \text{tai} \quad \parallel :3$$

$$3x = \underbrace{\pi - 0,25268}_{\text{}} + n2\pi$$

$$V: \begin{cases} x = 0,084 + \frac{n2\pi}{3} \\ x = 0,967 + \frac{n2\pi}{3} \end{cases}$$

$$302. \quad a) \quad \sin \frac{x}{5} = \sin 250^\circ$$

↓ MAOL

$$\frac{x}{5} = 250^\circ + n \cdot 360^\circ \quad // \text{tai} \quad \frac{x}{5} = 180^\circ - 250^\circ + n \cdot 360^\circ$$

$$\underline{\underline{x = 1250^\circ + n \cdot 180^\circ}}$$

$$\frac{x}{5} = -70^\circ + n \cdot 360^\circ \quad // \cdot 5$$

$$\underline{\underline{x = -350^\circ + n \cdot 180^\circ}}$$

$$304. \quad a) \quad \sin \alpha = \frac{\sqrt{3}}{2}$$

$$\sin \alpha = \sin \frac{\pi}{3}$$

$$\underline{\underline{\alpha = \frac{\pi}{3} + n \cdot 2\pi}} \quad \text{tai}$$

$$\text{MAOL: } \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$\alpha = \pi - \frac{\pi}{3} + n \cdot 2\pi$$

$$\underline{\underline{\alpha = \frac{2}{3}\pi + n \cdot 2\pi}}$$

$$308. a) \quad 2 \cdot \sin \left(x - \frac{\pi}{3} \right) = -\sqrt{3} \quad | :2$$

$$\sin \left(x - \frac{\pi}{3} \right) = -\frac{\sqrt{3}}{2}$$

$$\text{MAOL: } \sin \frac{4}{3}\pi = -\frac{\sqrt{3}}{2}$$

$$\sin \left(x - \frac{\pi}{3} \right) = \sin \left(\frac{4}{3}\pi \right)$$

*x ja y MAOL:in
kaavaan nro 48*

$$x - \frac{\pi}{3} = \frac{4}{3}\pi + n2\pi$$

$$\text{tai } x - \frac{\pi}{3} = \pi - \frac{4}{3}\pi + n2\pi$$

$$\underline{x = \frac{5}{3}\pi + n2\pi}$$

$$x = 0 + n2\pi$$

$$\underline{x = n2\pi}$$

310. a) $\underline{\underline{\sin\left(x + \frac{\pi}{4}\right) = \cos\left(\frac{\pi}{6} - x\right) = \sin\left(\frac{\pi}{2} - \left(\frac{\pi}{6} - x\right)\right)}$

MAOL: $\cos x = \sin\left(\frac{\pi}{2} - x\right)$

$$\sin\left(x + \frac{\pi}{4}\right) = \sin\left(x + \frac{\pi}{2} - \frac{\pi}{6}\right)$$

$$\sin\left(x + \frac{\pi}{4}\right) = \sin\left(x + \frac{\pi}{3}\right)$$

$$x + \frac{\pi}{4} = x + \frac{\pi}{3} + n2\pi \quad \text{tai} \quad x + \frac{\pi}{4} = \pi - \left(x + \frac{\pi}{3}\right) + n2\pi$$

x : + supisthu
→ ei ratk.

$$x + \frac{\pi}{4} = \pi - x - \frac{\pi}{3} + n2\pi$$

$$2x = \pi - \frac{\pi}{4} - \frac{\pi}{3} + n2\pi \quad \parallel : 2$$

$$\underline{\underline{V: x = \frac{5\pi}{24} + n\pi}}$$

$$313. \quad \cos^2 x - \sin x = \frac{1}{4}$$

MAOL: $\sin^2 x + \cos^2 x = 1$
 $\cos^2 x = 1 - \sin^2 x$

$$1 - \sin^2 x - \sin x = \frac{1}{4}$$

$$\sin^2 x + \sin x - \frac{3}{4} = 0$$

siis $t = \sin x$

$$\rightarrow t^2 + t - \frac{3}{4} = 0 \quad || \cdot 4$$

$$4t^2 + 4t - 3 = 0$$

$$t = \frac{-4 \pm \sqrt{16 - 4 \cdot 4 \cdot (-3)}}{8} = \frac{-4 \pm \sqrt{64}}{8} = \frac{-4 \pm 8}{8}$$
$$\begin{cases} = \frac{1}{2} \\ = -1,5 \end{cases}$$

S. 42: 302 b, 304 b,
308 b, 310 b,
312, 314

1) $\sin x = \frac{1}{2}$ tai

2) $\sin x = -1,5$ ei ratk.

Yleinen ratkaisu:

$$\sin x = \sin \frac{\pi}{6}$$

$$x = \frac{\pi}{6} + n2\pi \text{ tai}$$

$$x = \pi - \frac{\pi}{6} + n2\pi$$

$$x = \frac{5\pi}{6} + n2\pi$$