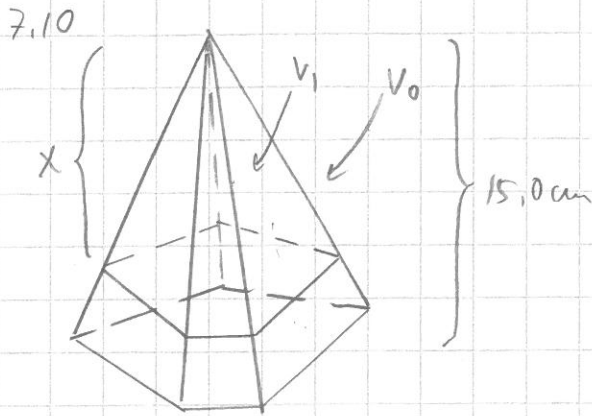


Olyjyn tilavuus:

$$V = A_{\text{poh}} \cdot h = 53,68,2 \text{ dm}^2 \cdot 35 \text{ dm} = 1878,841 \text{ dm}^3 \approx \underline{1900 \text{ l}}$$



$$V_1 \sim V_0$$

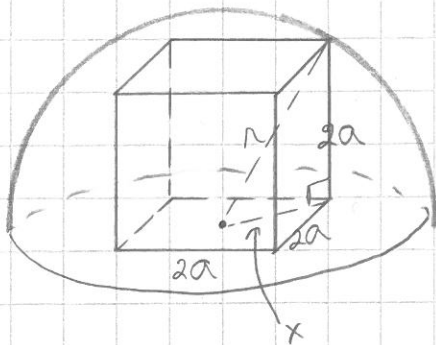
$$\frac{V_1}{V_0} = k^3 = \left(\frac{x}{15,0 \text{ cm}}\right)^3 = \frac{1}{2} \quad | \sqrt[3]{\quad}$$

$$\Rightarrow \frac{x}{15,0 \text{ cm}} = \sqrt[3]{\frac{1}{2}} \quad | \cdot 15,0 \text{ cm}$$

$$\Rightarrow x = 15,0 \text{ cm} \cdot \sqrt[3]{\frac{1}{2}} \approx 11,905 \text{ cm} \approx \underline{11,9 \text{ cm}}$$

$$\Rightarrow \text{alempi: } 15,0 \text{ cm} - x = \underline{3,1 \text{ cm}}$$

7.12



polyn korkeus:  $\sqrt{(2a)^2 + (2a)^2} = \sqrt{8a^2}$   
 $= \sqrt{4} \sqrt{2} \sqrt{a^2} = 2\sqrt{2}a$

$$x = \frac{1}{2} \cdot 2\sqrt{2}a = \sqrt{2}a$$

Pythagoras:  $(\sqrt{2}a)^2 + (2a)^2 = r^2$

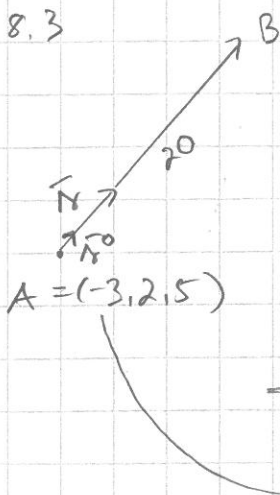
$$\Rightarrow 2a^2 + 4a^2 = r^2$$

$$\Rightarrow 6a^2 = r^2 \quad | \sqrt{\quad}$$

$$\Rightarrow r = \sqrt{6a^2} = \sqrt{6}a$$

$$\frac{V_k}{V_{\frac{1}{2}r}} = \frac{(2a)^3}{\frac{1}{2} \cdot \frac{4}{3} \pi r^3} = \frac{8a^3}{\frac{2}{3} \pi (\sqrt{6}a)^3} = \frac{8a^3}{\frac{2}{3} \pi (\sqrt{6})^3 a^3} \approx 0,2598 \approx 26\%$$

8.3



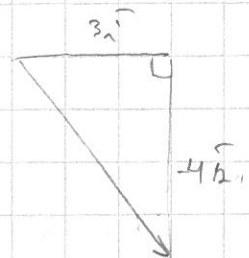
$$\vec{r} = 3\vec{i} - 4\vec{k}$$

$$|\vec{r}| = \sqrt{3^2 + (-4)^2} = 5$$

$$\vec{AB} = 20 \frac{\vec{r}}{|\vec{r}|} = 20 \frac{\vec{r}}{5} = 20 \cdot \frac{\vec{r}}{5}$$

$$= 4\vec{r} = 4(3\vec{i} - 4\vec{k}) = 12\vec{i} - 16\vec{k}$$

$$\Rightarrow B = (-3 + 12, 2 + 0, 5 - 16) = \underline{(9, 2, -11)}$$



8.14

$$\vec{c} = \vec{i} + 7\vec{j}$$

$$\vec{a} = 2\vec{i} + 3\vec{j}$$

$$\vec{b} = -7\vec{i} + 6\vec{j}$$

$$\vec{c} = x\vec{a} + y\vec{b}$$

$$\Rightarrow \vec{i} + 7\vec{j} = x(2\vec{i} + 3\vec{j}) + y(-7\vec{i} + 6\vec{j})$$

$$= 2x\vec{i} + 3x\vec{j} - 7y\vec{i} + 6y\vec{j}$$

$$= (2x - 7y)\vec{i} + (3x + 6y)\vec{j}$$